

Student Code Number: _____

Ph.D. Qualifying Exam

INTERMEDIATE SOLID & STRUCTURAL MECHANICS

Spring 2013

**Prof. D. Liu
Prof. R. Averill**

Directions: Open Book, one book and one notebook allowed.

Answer all four questions

All questions have equal weight

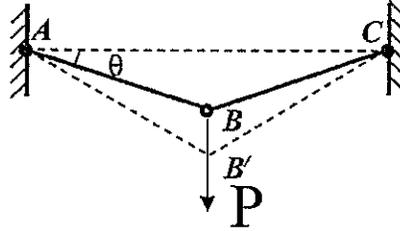
Time: 3.0 hrs.

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- If you make any assumption to reach a solution, state it clearly.
- Assume and state the approximate values for properties, if needed and used.

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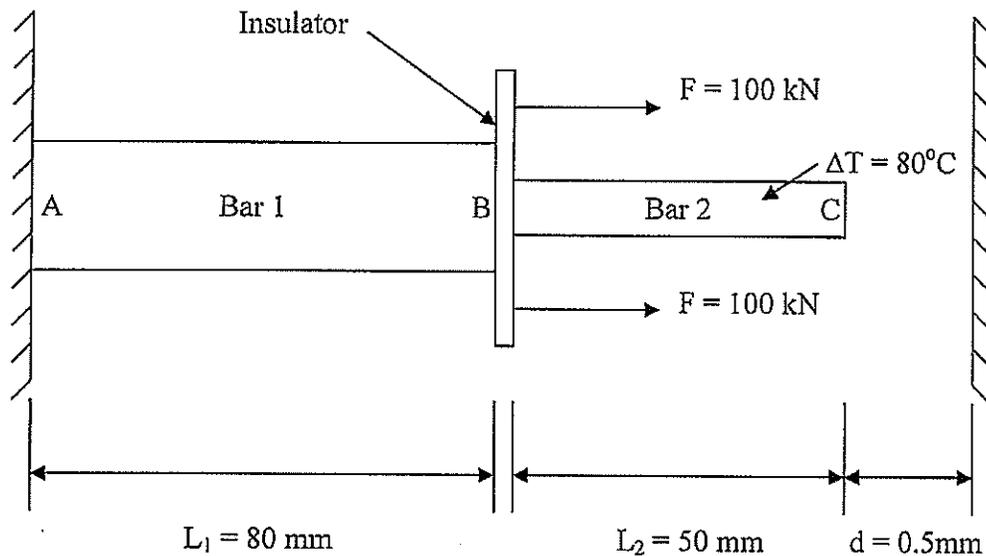
1. A structure consisting of two equal steel bars 15 feet long and with hinged ends is subjected to the action of a vertical load P . Assume Young's modulus of the bars is 29 Msi. Determine the cross sectional areas of the bars and the vertical deflection of point B when $P=5000$ lbs. The allowable stress is $\sigma_{\text{all}}=10,000$ lbs/in², and the initial angle of inclination of the bars $\theta = 30^\circ$.



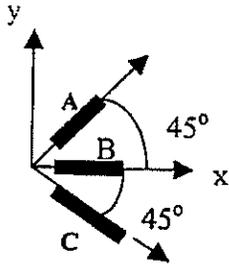
2. The stepped bar shown below is fixed at point A and is initially free at point C. At point B, a thin, rigid insulator separates bar 1 from bar 2. Bar 1 is made of steel, with Young's modulus $E_1 = 200 \text{ GPa}$, cross-sectional area $A_1 = 100 \text{ mm}^2$, and length $L_1 = 80 \text{ mm}$. Bar 2 is made of aluminum, with Young's modulus $E_2 = 72 \text{ GPa}$, coefficient of thermal expansion $\alpha_2 = 23 \times 10^{-6}$ per degree C, cross-sectional area $A_2 = 60 \text{ mm}^2$, and length $L_2 = 50 \text{ mm}$. Two mechanical loads $F = 100 \text{ kN}$ are applied at point B, and a thermal load $\Delta T = 80$ degrees C is applied to bar 2 only. After the loading is applied:

- determine whether or not point C contacts the fixed wall to the right,
- determine the stresses in bar 1 and bar 2, and
- decide if the stresses in part (b) seem reasonable.

Hooke's law for one-dimensional thermo-mechanical loading: $\sigma = E(\epsilon - \alpha\Delta T)$



The readings from a strain gage rosette are as follows: $\epsilon_A = 520 \times 10^{-6}$, $\epsilon_B = 360 \times 10^{-6}$ and $\epsilon_C = -80 \times 10^{-6}$. Determine the principal strains and the maximum shear strain.



$$\epsilon_x' = \frac{\epsilon_x + \epsilon_y}{2} + \frac{\epsilon_x - \epsilon_y}{2} \cos 2\theta + \frac{\gamma_{xy}}{2} \sin 2\theta$$

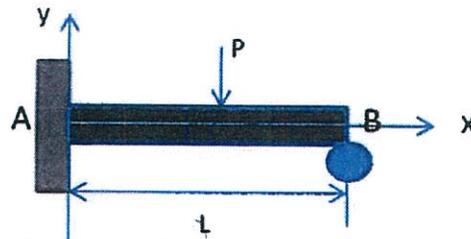
$$\epsilon_y' = \frac{\epsilon_x + \epsilon_y}{2} - \frac{\epsilon_x - \epsilon_y}{2} \cos 2\theta - \frac{\gamma_{xy}}{2} \sin 2\theta$$

$$\gamma_{xy}' = -\frac{\epsilon_x - \epsilon_y}{2} \sin 2\theta + \frac{\gamma_{xy}}{2} \cos 2\theta$$

Suggested solution procedures:

- (A) Express the three strain components in the x-y coordinate system, i.e. ϵ_x , ϵ_y and γ_{xy} , in terms of ϵ_A , ϵ_B and ϵ_C .
- (B) Find the values of the strain components ϵ_x , ϵ_y and γ_{xy} .
- (C) Find the principal strain and the maximum shear strain based on Mohr's circle analysis.

The beam AB shown below is fixed at point A and simply supported at point B. Based on the formula given inside the block, determine the reaction forces at A and B.



$$v = \frac{-Px^2}{6EI} (3l-x)$$

Suggested solution procedures:

- (A) Give a free-body diagram.
- (B) Present the equilibrium equations based on loading P and reaction forces.
- (C) Show principle of superposition for linear analysis with diagrams.
- (D) Give the compatibility equation.
- (E) Find the deflection at point B due to the concentrated force P.
- (F) Find the reaction forces at A and B.