

**Code Number :.....**

# **HEAT TRANSFER QUALIFYING EXAM**

August 2018

**One book allowed (closed notes)**

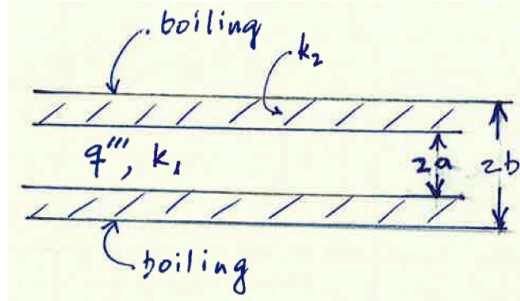
Answer all questions

All questions have equal weight

TIME: 3.0 hrs

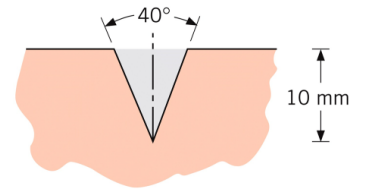
Prepared by Profs. N. Wright and J. Yeom

**Problem 1** A laminated plate consists of an internal layer of metal ( $-a \leq x \leq +a$ ) sandwiched by layers of a different metal ( $-b \leq x \leq -a$  and  $a \leq x \leq b$ ). The inner layer is 2 cm thick ( $a = 1$  cm) and has a thermal conductivity of  $50 \text{ W m}^{-1} \text{ K}^{-1}$  and volumetric heat generation of  $10^6 \text{ W m}^{-3}$ . The outer layers are 1 cm thick and in perfect contact with the inner layer. The outer layers have conductivity of  $20 \text{ W m}^{-1} \text{ K}^{-1}$  and no heat generation. The plate is immersed in water at 1 atm. Assuming that the water at the outer surface of the plate is subject to pool boiling (i.e., assume a very large value of the heat transfer coefficient  $h$ ) and that the thickness of the cladding on each side is 1 cm, determine the steady-state temperature 1) at the centerline of the plate and 2) at the interface of the two solid materials.



**Problem 2.** Consider a thin walled pipe made of a highly conducting metal. The pipe has a diameter of 5 cm. Water enters at 57 °C and exits at 47 °C with a mass flow rate of  $\dot{m} = 0.25 \text{ kg s}^{-1}$ . Air at 20 °C flows across the pipe at a velocity of 10 m s<sup>-1</sup>. Estimate the length of the pipe needed to achieve these conditions.

- Problem 3.** Consider a long V groove that is 10 mm deep machined on a block. The block is maintained at 727°C. The groove surfaces are opaque and diffuse for which  $\alpha_\lambda = 0.85$  for  $\lambda \leq 3 \mu\text{m}$ ,  $\alpha_\lambda = 0.57$  for  $3 \mu\text{m} < \lambda \leq 5 \mu\text{m}$ , and  $\alpha_\lambda = 0.15$  for  $\lambda > 5 \mu\text{m}$ .
- (a) Determine the total emissivity of the groove surface.
- (b) Compute the radiant flux leaving the groove to its surroundings at 27°C.



**Problem 4.** Consider an array of vertical rectangular fins used to cool an electronic device mounted in quiescent, atmospheric air at  $T_\infty = 27^\circ\text{C}$ . Each fin has the length of  $L = 30\text{ mm}$  and the height of  $H = 200\text{ mm}$ . The fin base temperature is maintained at  $T_b = 127^\circ\text{C}$ . The fin is made of aluminum with  $k = 205\text{ W/m}\cdot\text{K}$ .

- Viewing each fin surface as a vertical plate in an infinite, quiescent medium, estimate the optimum value of a fin spacing  $S$  for the prescribed condition.
- Calculate the heat transfer coefficient assuming that the surface of each fin ( $T_s = 127^\circ\text{C}$ ) is at the uniform temperature, which is the same as the base temperature.
- Using the computed “ $h$ ” from (b) and for the optimum value of  $S$  and a fin thickness of  $t = 1.6\text{ mm}$ , estimate the heat transfer rate from the fin array (including the prime surface) of width  $W = 350\text{ mm}$ . For Part (c), the fin array is no longer at the constant temperature, and the temperature decrease along the fin length should be accounted for.

